

# A Tutorial for Competent Memetic Algorithms: Model, Taxonomy, and Design Issues

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# Three Kinds of Evolution Theory

- Lamarck evolution: If an organism changes during life in order to adapt to its environment, those changes are passed on to its offspring.
- Darwin evolution: The desires of animals have nothing to do with how they evolve, and that changes in an organism during its life do not affect the evolution of the species.
- Baldwin effect: It proposed that the ability of individuals to learn can guide the evolutionary process, facilitating evolution by smoothing the fitness landscape.

# Evolution Algorithms and Local Search

- EAs are a class of search and optimization techniques based on Darwinian Evolution.
- Solutions are encoded as so-called chromosomes. Crossover, mutation, and selection are proceeded on chromosomes to obtain a better solution.
- Pure EAs are not well suited to fine tuning search in complex combinatorial spaces. Hybridization with other techniques can greatly improve the efficiency of search.

# Memetic Algorithms

- The combination of EAs with local search (LS) was named memetic algorithms (MAs).
- The choice of name is inspired by Richard Dawkins' concept of a “meme”, which represents a unit of cultural evolution that can exhibit local refinement.
- In the literature, MAs have also been named hybrid genetic algorithms (GAs), genetic local searches, Lamarckian GAs, and Baldwinian GAs.

# Goals, Aims, and Methods

- This paper aims to begin the process of placing MA design on a sounder footing.
- The first goal is to define a syntactic model which enables a better understanding of the interplay between the different component parts of an MA.
- With such a model , we can construct a taxonomy of MAs, the second goal of this paper.

# Design Issues for MAs

- Where and when should local search be applied within evolutionary cycle?
- Which individuals in the population should be improved by local search, and how should they be chosen?
- How much computational effort should be allocated to each local search?
- How can the genetic operators best be integrated with local search in order to achieve a synergistic effect?

# TSP Problem definition

- Instance: A set  $C$  of  $m$  cities, and there are some paths between cities.
- Solution: a tour of  $C$  (a permutation from  $[1 \dots m]$  to  $[1 \dots m]$ ).
- Measure: the length of the tour.
- Aim: minimum length tour.

## 1997 Handbook of Evolutionary Computation

T.Back, D.Fogel, and Z.Michalewicz

*Genetic\_Local\_Search*( $P \in S^t$ )**Begin**/\*  $\lambda, \mu, m \geq 1$  \*/**For**  $i := 1$  **To**  $\mu$  **Do**Iterative\_Improvement ( $s_i$ );**Od**

stop\_criterion := false

**While** ( $\neg$  stop\_criterion) **Do** $P' := \emptyset$ ;**For**  $i := 1$  **To**  $\lambda$  **Do**

/\* Mate \*/

 $M_i \in P^m$ ;

/\* Recombine \*/

 $s_i \in H_m(M_i)$ ;Iterative\_Improvement ( $s_i$ ); $P' := P' \cup \{s_i\}$ ;**Od**

/\* Select \*/

 $P := (P \cup P')^\mu$ ;

evaluate stop\_criterion

**Od****End.**

Local Search

No Mutation

 $(\mu + )$ -selection



# 1999 Memetic Algorithms using guided local search: a case study

D.Corne, F.Glover, and M.Dorigo

1. The local search is used after every genetic operators.
2. Also  $(\mu + )$ -selection.
3. Double function evaluation

*GLS\_Based\_Memetic\_Algorithm*

**Begin**

Initialize population;

**For**  $i := 1$  **To**  $\text{sizeOf}(\text{population})$  **Do**

$\text{individual} := \text{population}_i$ ;

$\text{individual} := \text{Local} - \text{Search} -$

$\text{Engine}(\text{individual})$ ;

$\text{Evaluate}(\text{individual})$ ;

**Od**

**Repeat Until** (termination\_condition)

**Do**

**For**  $j := 1$  **To** #recombinations **Do**.

$\text{selectToMerge}$  a set  $S_{\text{par}} \subseteq$

population;

$\text{offspring} = \text{Recombine}(S_{\text{par}}, x)$ ;

$\text{offspring} = \text{Local} - \text{Search} -$

$\text{Engine}(\text{offspring})$ ;

$\text{Evaluate}(\text{offspring})$ ;

Add offspring to population;

**Od**

**For**  $j := 1$  **To** #mutations **Do**

$\text{selectToMutate}$  an individual in  
population;

$\text{Mutate}(\text{individual})$ ;

$\text{individual} = \text{Local} - \text{Search} -$

$\text{Engine}(\text{individual})$

$\text{Evaluate}(\text{individual})$ ;

Add individual to population;

**Od**

$\text{population} = \text{SelectPop}(\text{population})$ ;

**If** (population has converged) **Then**

$\text{population} = \text{RestartPop}(\text{population})$ ;

**Fi**

**Od**

**End.**

1996 A genetic local search algorithm for solving symmetric and asymmetric traveling salesman problems

B.Freisleben and P.Merz

1. Good operator or good MA?
2. Local search between mutation and crossover

*STSP-GA*

**Begin**

Initialize pop  $P$  with

Nearest-Neighbor(...);

**For**  $i := 1$  **To**  $\text{popsize}(P)$  **Do**

$\text{Lin} \leftarrow \text{Kernighan} - \text{Opt}(\text{individual}_i), i \in P;$

**od**

**Repeat Until** (converged) **Do**

**For**  $i := 0$  **To**  $\# \text{crossover}$  **Do**

        Select two parents  $i_a, i_b \in P$

        randomly;

$i_c = \text{DPX} - \text{STSP}(i_a, i_b);$

$\text{Lin} \leftarrow \text{Kernighan} - \text{Opt}(i_c);$

        With probability  $m_p$  do

        Mutation-STSP ( $i_c$ );

        Replace an individual of  $P$  by  $i_c$ ;

**od**

**od**

**End.**

Special crossover

Special mutation

# QAP Problem definition

- Instance:  $A, B$  matrices of  $n \times n$
- Solution: A permutation  $\pi$  on  $n$
- Measure: The cost of permutation
$$C(\pi) = \sum_{i=1}^n \sum_{j=1}^n a_{i,j} b_{\pi(i), \pi(j)}$$
- Aim: Minimum cost permutation

## 1993 Genetic hybrids for the quadratic assignment problem

C.Fleurent and J.Ferland

1. H1 and H2 both are Tabu search
2. Cull is a  $(\mu + )$ -selection.
3. No mutation

*Genetic\_Hybrid\_Algorithm*( $H_1, H_2$ )**Begin** $P := \emptyset;$ **For**  $i := 1$  **To**  $m$  **Do**    generate a random permutation  $p$ ;    Add  $H_1(p)$  to  $P$ ;**od**Sort  $P$ ;**For**  $i := 1$  **To** number\_of\_generations **Do**    **For**  $j := 1$  **To** num\_offspring\_per\_    generation **Do**        select two parents  $p_1, p_2$  from  $P$ ;         $child := crossover(p_1, p_2);$         Add  $H_2(child)$  to  $P$ ;    **od**    Sort  $P$ ;    Cull( $P, num\_offspring\_per\_generation$ );**od**Return the best  $p \in P$ ;**End.**

# 1999 A comparison of memetic algorithms, tabu search, and ant colonies for the quadratic assignment

C.Fleurent and J.Ferland

```

QAP_MA
Begin
  Initialize population  $P$ ;
  For  $i := 1$  To  $\text{sizeof}(P)$  Do
     $\text{individual} := P_i$ ;
     $\text{individual} := \text{Local\_Search}(\text{individual})$ ;
  Od
  Repeat Until (terminate=True) Do
    For  $i := 1$  To #recombinations Do
      Select two parents  $i_a, i_b \in P$ 
      randomly;
       $i_c := \text{Recombine}(i_a, i_b)$ ;
       $i_c := \text{Local\_Search}(i_c)$ ;
      Add individual  $i_c$  to  $P$ ;
    Od
     $P := \text{Select}(P)$ ;
    If ( $P_{\text{converged}}$ ) Then
      For  $i := 1$  To  $\text{sizeof}(P)$ ,  $i \neq \text{index}(\text{Best})$ 
      Do
         $\text{individual} := P_i$ ;
         $\text{individual} := \text{Local\_Search}(\text{Mutate}(\text{individual}))$ ;
      Od
    Fi
  Od
End.
  
```

1. Use mutation to prevent convergence
2.  $(\mu + )$ -selection

# MGC Problem definition

- Instance: Graph  $G = (V, E)$
- Solution: A coloring of  $G$
- Measure: cardinality  $k$  of coloring
- Aim: Minimum  $k$  coloring

## 1998 A new genetic local search algorithm for graph coloring

C.Fleurent and J.Ferland

*GL\_for\_Coloring***Begin**

```

/* f, F*: fitness function and */
/* best value encountered so far */
/* s*: best individual encountered so far */

```

```

/* best(P): returns the best individual */

```

```

/* of the population P */

```

```

i = 0;

```

```

generate( $P_0$ );

```

```

 $s^* := best(P_0)$ ;

```

```

 $f^* := f(s^*)$ ;

```

```

While ( $f^* > 0$  and  $i < maxIter$ ) Do

```

```

     $P'_i := crossing(P_i, T_x)$ ;

```

```

    /* using specialised crossover */

```

```

     $P_{i+1} = mutation(P'_i)$ ;

```

```

    /* using Tabu search */

```

```

    If ( $f(best(P_{i+1})) < f^*$ ) Then

```

```

         $s^* := best(P_{i+1})$ ;

```

```

         $f^* := f(s^*)$ ;

```

```

    Fi

```

```

    i := i + 1;

```

```

Od

```

**End.**

1. Mutation is replaced by Tabu search
2. For some large instance, have the best results
3. No survivor selection

# PSP Problem definition

- Instance: A simplified protein sequence of length  $l$   
i.e., a string  $s \in \{G, P\}^l$
- Solution: A self-avoiding path  $p$  which embeds  $s$  into a two or three dimensional lattice.
- Measure: Potential energy
$$E(p) = - \sum_{i=1}^l \sum_{j=i+1}^l D_{ij} | (D_{ij} = 1) \wedge (s_i = s_j = H)$$
- Minimum energy solution



## 2000 A memetic algorithm with self-adaptive local search: TSP as a case study

K.Krasnogor and J.Smith

```
PF_MA
Begin
  Random initialize population Parents;
  Repeat Until (Finalization_cri-
    teria_met) Do
    Local_Search(Parents);
    mating_pool=Select_mating(Parents);
    offsprings:=Cross(mating_pool);
    Mutate(offsprings)
    Parents:=Select(Parents+offsprings)
  Od
End.
```

1. ( $\mu +$  )-selection

# Syntactic Model

- Simple EAs
- Coordinating local search with crossover and mutation
- Coordinating local search with population management
- Incorporation historical information

# Taxonomy

$$D(A) = b_{mS} b_{cS} b_R b_M$$

$b_{mS}$ : provide history data to its local search

$b_{cS}$ : provide population statics to its local search

$b_R$ : corporate with recombination

$b_M$ : corporate with mutation

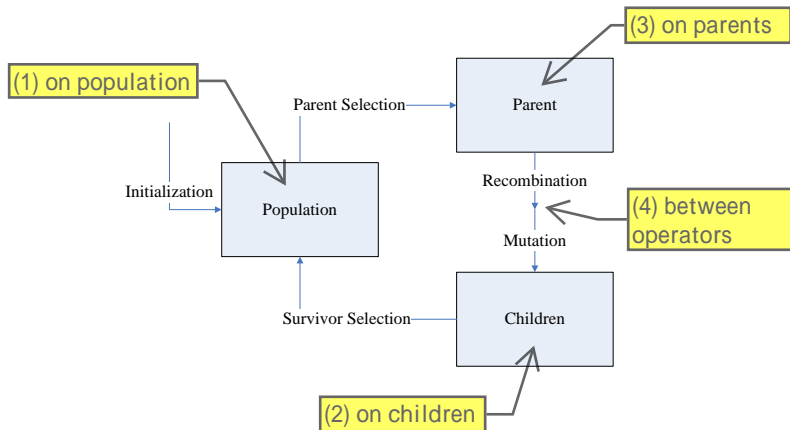
TABLE I  
CLASSIFICATION OF ALGORITHMS DISCUSSED IN SECTION III ACCORDING TO PROBLEM AND  $D$

|          |                              |      |            |      |                         |                        |                    |
|----------|------------------------------|------|------------|------|-------------------------|------------------------|--------------------|
| 9 - 15   |                              |      |            |      |                         |                        |                    |
| 8        |                              |      |            |      |                         |                        | [21]               |
| 7        |                              |      |            |      |                         | [76]                   | [82]               |
| 6        |                              | [16] |            | [47] |                         |                        |                    |
| 5        |                              |      |            |      |                         |                        | [83]               |
| 4        | [57]                         |      |            |      | [57], [59]              | [26], [74], [84], [85] |                    |
| 3        | [13], [38], [44]             |      |            |      |                         | [86]                   | [87], [88]         |
| 2        | [37], [42], [43], [45], [46] | [9]  | [50], [51] |      |                         |                        |                    |
| 1        |                              |      | [49]       |      |                         |                        | [89], [90]         |
| 0        |                              |      |            |      |                         |                        |                    |
| <b>D</b> | TSP                          | QAP  | MGC        | BPQ  | PFP and Protein Docking | General Studies        | Other Applications |

# Choice of Local Search Operators

- The answer is “it depends”. Even within a single problem class (like TSP), the choice of LS operators was instance-dependent.
- It is trivially true that a point which is locally optimal with respect to one operator may not be with respect to another. Multiple local search operators may be work (variable neighborhood search).
- Using multiple operator may be inefficiency and adapting the parameters of LS is useful. But adaptation of parameters produces noise in a first-ascent approach.

# Integration Into EA Cycles



# Managing the Global-Local Search Tradeoff

- Most MAs apply local search to every individual in every generation of the EA.
- Hart(1994) and Land(1998) suggest various mechanisms to choose individuals to be optimized, the intensity of local search and the probability of performing LS.
- Land(1998) proposes the use of fine-grain schedulers that sample the basin of attraction. Only those solutions that are in promising basin of attraction will be assigned later.

# Conclusion

- The syntactical model obtained allowed for the definition of an index number  $D$ .
- When plotting the  $D$  index for a number of papers, we were able to identify classes of MAs that had received a lot of attention and other classes that were little explored.